

# *Nuclear Resonance Photon Scattering Studies of N<sub>2</sub> Adsorbed on Grafoil and of NaNO<sub>2</sub> Single Crystal*

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The nuclear resonance photon scattering (NRPS) from <sup>15</sup>N<sub>2</sub> adsorbed on graphite was investigated. The resonantly scattered intensities from the 6324 keV level of <sup>15</sup>N with the photon beam parallel and perpendicular to the adsorbing grafoil planes was measured at 140 K and coverages below 0.7 monolayers (ML), where the <sup>15</sup>N<sub>2</sub> occur in the *vapor phase*. The data were used for deducing the out-of-plane tilt angle of adsorbed N<sub>2</sub> relative to the graphite surface and the results were compared with grand canonical Monte Carlo (GCMC) calculations. Using the same method, a single crystal of NaNO<sub>2</sub> was studied by measuring the scattering intensities with the nitrite planes aligned parallel and perpendicular to the

photon beam. At 80 K, a huge anisotropy ( $R \approx 3.6$ ) was observed, caused by the anisotropy in the zero-point motion of the internal modes of vibration of the NO<sub>2</sub> ion. The variation of the scattering intensity from a powdered isotopic <sup>15</sup>NaNO<sub>2</sub> sample versus  $T$  in the range 12 K to 297 K was also measured and explained by accounting for the internal and external vibrational modes in NaNO<sub>2</sub>.

**Key words:** effective temperature; gas adsorption; lattice modes; (n, $\gamma$ ) reaction; normal modes; nuclear resonance photon scattering; zero-point energy.

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## **1. Introduction**

The Doppler broadening of nuclear levels caused by the zero-point vibrations and thermal motion have been used for measuring the zero-point kinetic energies and linear momenta of atoms in solids and in adsorbed molecules on surfaces. This was done using nuclear resonance photon scattering (NRPS) from the 6324 keV level of <sup>15</sup>N in N-containing molecules [1], and was applied for studying molecular orientations [2] in a variety of anisotropic systems [3-6]. We hereby report the results of two recent studies.

Physical adsorption of N<sub>2</sub> monolayers on graphite (in the form of Grafoil) is probably the most studied system in relation to 2-dimensional (2D) physics; it was extensively studied using several techniques, such as n-diffraction, low-energy-electron diffraction, x-ray diffraction, adsorption isotherms and specific heats [7-11]. These studies yielded the in-plane orientational ordering and phase diagrams at temperatures below the

2D tricritical point ( $T_c \approx 85$  K), i.e., in the solid and liquid phases. One interesting feature, almost uncovered by the above experimental techniques, is the study of the *out-of-plane* tilt angle of the N<sub>2</sub> molecular axis relative to the adsorbing graphite planes. At high temperatures, all diffraction techniques fail to yield any useful information concerning this topic. In this respect, the NRPS technique [1] is unique as it is the only technique which provides direct information on the tilt of N<sub>2</sub> molecules relative to the graphite planes, not only in the fluid phase but also in the vapor phase.

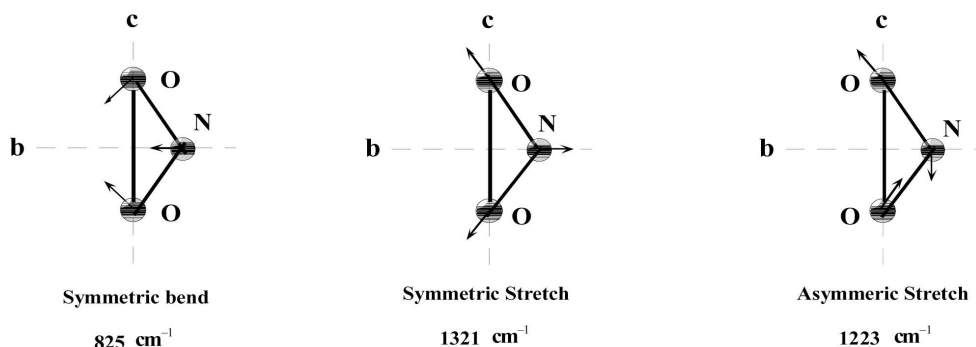
NaNO<sub>2</sub> is a molecular solid; the nitrite ions (NO<sub>2</sub><sup>-</sup>) in a single crystal are all parallel to each other; the NaNO<sub>2</sub> has nine vibrational modes [12]: three internal modes ( $825\text{ cm}^{-1} < \nu < 1321\text{ cm}^{-1}$ ) confined to the NO<sub>2</sub><sup>-</sup> *ionic plane* (Fig. 1), and six external modes of the lattice (of Na<sup>+</sup> against NO<sub>2</sub><sup>-</sup>) which occur in the  $120\text{ cm}^{-1}$  to  $220\text{ cm}^{-1}$  spectral region. The internal modes

(which are all planar) are the main contributors to the zero-point motion, making the single crystal highly anisotropic. It is interesting to find out to what extent this anisotropy could be reproduced by experiment.

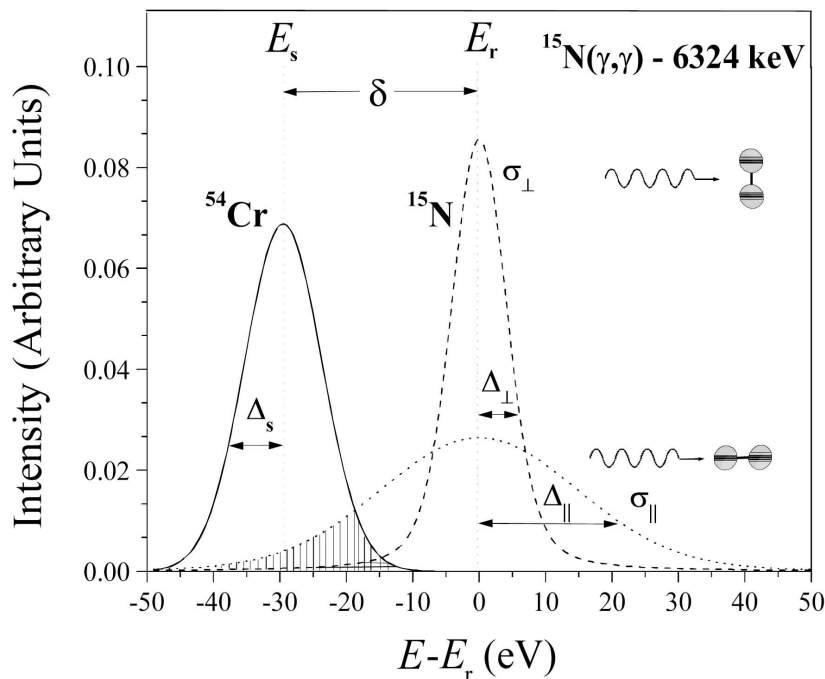
### 1.1 The NRPS Technique

The basic idea of the NRPS method relies on monitoring the Doppler broadening of the nuclear level in  $^{15}\text{N}$  caused not only by the thermal motion but also by the internal *zero-point* vibrational motion of the N-atom. This technique uses a photon beam generated by the  $\text{Cr}(n,\gamma)$  reaction with neutrons obtained from a

nuclear reactor. It so happens that the  $\gamma$ -line of  $^{54}\text{Cr}$  overlaps by chance [1] (within  $\delta = 29.5$  eV) the 6324 keV nuclear level of  $^{15}\text{N}$ . The overlapping process is such that the resonance scattering cross section is proportional to the Doppler broadening of the nuclear level,  $\Delta_r = E(2kT_r/M_r c^2)^{1/2}$ , where  $E$ , the excitation energy,  $M_r$ , the nuclear mass,  $T_r$ , the effective temperature of the scattering atom,  $k$ , the Boltzmann constant, and  $c$  the velocity of light. It may be noted that  $T_r$  expresses the *total kinetic* energy of the scattering atom, including the part associated with its internal zero-point vibrational motion. This situation is schematically illustrated in Fig. 2 for the parallel and perpendicular



**Fig. 1.** Internal normal modes of  $\text{NO}_2$  taken from Ref. [12]. Vectorial arrows represent atomic motions. Note that all modes are confined to the  $\text{NO}_2$  plane ( $b,c$ ).



**Fig. 2.** Calculated shape of the Doppler-broadened level at 6324 keV in  $^{15}\text{N}$  of peak energy  $E_r$  and of the Doppler-broadened incident line of the  $^{54}\text{Cr}(n,\gamma)$  reaction of peak energy  $E_s$  (after recoil correction), for  $T_s = 460$  K. The nuclear level shape is depicted for ideal cases calculated at  $T = 0$  K, with the molecular  $\text{N}_2$  symmetry axis positioned parallel and perpendicular to the photon beam. The corresponding Doppler widths  $\Delta_s$ ,  $\Delta_{\parallel}$  and  $\Delta_{\perp}$  of the three lines are indicated. The overlap integrals between the shape of the incident line and the nuclear level are shown as shaded areas and are related to the scattering cross sections  $\sigma_{\parallel}$  and  $\sigma_{\perp}$ .

orientations of the  $N_2$  molecular axis with respect to the  $\gamma$ -beam direction. The diatomic  $N_2$  molecule is highly anisotropic; the total kinetic energy of the N-atom is maximum along the  $N_2$  molecular axis (containing the internal vibrational motion) and minimum in the perpendicular direction. Hence the Doppler broadening of the  $^{15}N$  nuclear level should have a maximum,  $\Delta_{\parallel}$ , along the  $N_2$  symmetry axis and a minimum,  $\Delta_{\perp}$ , along the perpendicular direction. The corresponding scattering cross sections  $\sigma_{\parallel}$  and  $\sigma_{\perp}$  are proportional to the overlap integrals (shown as the shaded areas in Fig. 2) and fulfill the relation  $\sigma_{\parallel} \gg \sigma_{\perp}$ . Here, we utilize this dependence of the scattering cross section  $\sigma_r$  on the orientation of  $N_2$  with respect to the photon beam, for measuring the out-of-plane tilt angle of the  $N_2$  molecular axis with respect to the adsorbing graphite planes. Similarly, the anisotropy in the scattered intensities from the  $NaNO_2$  single crystal, reflects the anisotropy of the  $NO_2^-$  internal modes; all of which are confined to the nitrite ionic plane. Thus, the total kinetic energy of the N-atom has a maximum along the  $NO_2^-$  plane and a minimum along the normal to the plane.

## 2. Experimental Details

### 2.1 The $\gamma$ -Source

The  $\gamma$ -source was generated from the  $(n,\gamma)$  reaction on three chromium disks (each 8 cm diameter and 1.5 cm thick) placed along a tangential beam tube near the core of the IRR-2 reactor. The photon beam was collimated and neutron filtered through 40 cm of borated paraffin before hitting the scatterer. The scattered photons were detected using two hyperpure Germanium (HPGe) detectors, with efficiencies of 35 % and 30 %, set 15 cm from the sample at scattering angles of  $120^\circ$ . The detectors were shielded against low-energy scattered photons and background neutrons using 9 mm lead and 1 cm borated plastic. Other details concerning the experimental system are found elsewhere [13].

### 2.2 The $N_2$ -Grafoil Sample

The Grafoil cell consists of two thin-walled pure aluminum cylindrical compartments. The small one (40 mm i.d., 40 mm high, contains 40.5 g Grafoil consisting of 86 rectangular parallel sheets) is positioned in the path of the photon beam (see inset to Fig. 3), while the large one, serving as a gas reservoir, was outside the beam region. This design has the following advantages over the stainless steel cell of a previous work [2]: (i) the scattered background is reduced enormously. (ii) the scattered signal arises primarily from the adsorbed  $N_2$ , while the contribution of the free non-adsorbed gas is

very small. (iii) The Grafoil (purchased from Deutsch Carbon) is of a better quality in the sense that the product  $f \cdot \phi$  (where  $f = 0.30$  is the randomly oriented fraction of the crystallite surfaces and  $\phi = 30^\circ$  the FWHM angle of the mosaic spread) is now smaller by  $\approx 30\%$  compared to that of Ref. [2]. The cell was mounted inside a variable temperature cryostat (10 K to 300 K) which could be rotated around an axis coinciding with that of the Grafoil cylindrical cell from one position where the photon beam is parallel to the Grafoil planes of the sample to a perpendicular position. Isotopically enriched  $N_2$  (99 %  $^{15}N$ ) was used.

### 2.3 The $NaNO_2$ Samples

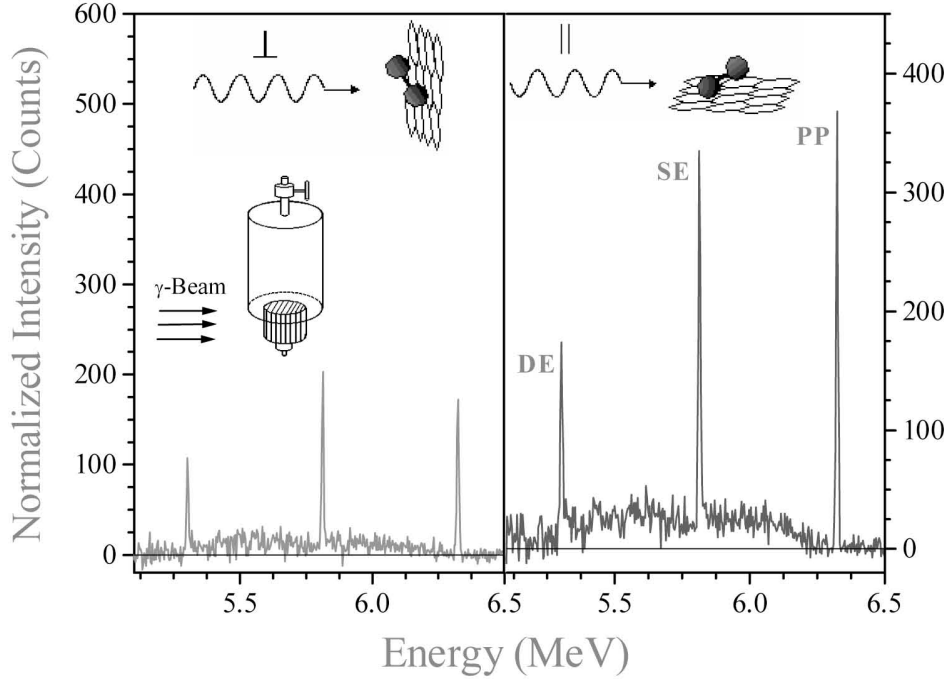
Two samples were used: a 1.03 g of *isotopic powdered*  $Na^{15}NO_2$  sample (99 %  $^{15}N$ ), placed in a thin walled, pure aluminum cylinder; it was used for measuring the scattered intensity versus  $T$ . The second, contained a  $\approx 7$  g *natural*  $NaNO_2$  single crystal (0.36 %  $^{15}N$ ) having only  $\approx 6$  mg  $^{15}N$ , was employed for measuring the scattered intensity ratios  $R = I_{\parallel}/I_{\perp}$  with the photon beam parallel and perpendicular to the  $NO_2^-$  planes of the single crystal whose orientation was determined using x-ray diffraction. Because of the very small amount of  $^{15}N$  ( $\approx 6$  mg) present in the sample, the scattered background had to be reduced by fitting the outer and inner radiation shields of the cryostat by four 0.02 mm thick aluminum coated Mylar windows. The  $NaNO_2$  crystal was covered with thin Al foil to facilitate thermal conduction at low  $T$ . Because of some technical difficulties, we did not measure the scattering from the single crystal below 80 K. The temperature was monitored using two thermocouples set at two extreme points of the samples.

## 3. Theoretical Remarks

As discussed in Sec. 1.1, the resonance scattering cross section is proportional to the Doppler broadening of the nuclear level, which in turn depends on the scatterer effective temperature  $T_r$ . It follows, that in order to predict the scattering cross sections, it was necessary to evaluate  $T_r$  of the N-atom for all scatterers in question. A detailed procedure for calculating  $T_r$  is given in Refs. [1] and [2]. We hereby give the method for evaluating the scattering cross section.

### 3.1 Resonance Scattering Cross Section

As illustrated schematically in Fig. 2, the resonance photon scattering process is caused by a Doppler broadened  $\gamma$ -line, represented by a Gaussian,  $F(E)$ , overlapping a Doppler broadened nuclear level at 6324 keV in  $^{15}N$ , represented by a  $\psi$ -function  $\psi(x,t)$ . The scattering



**Fig. 3.** Scattered radiation spectra (background subtracted) from the N<sub>2</sub>+Grafoil sample at  $T = 20$  K, with the  $\gamma$ -beam parallel ( $\parallel$ ) and perpendicular ( $\perp$ ) to the Grafoil planes, at a submonolayer coverage of 0.60 ML. The anisotropy ratio of the scattered intensities is  $R = I_{\parallel}/I_{\perp} = 1.97$ . The photo peak, single-escape and double-escape peaks are labelled PP, SE, and DE. The inset shows the sample container where the path of the  $\gamma$ -beam is indicated. The upper gas reservoir is not hit by the photon beam.

cross section, for an infinitely thin  $^{15}\text{N}$  sample, is given by the overlap integral (shown as the shaded area in Fig. 2). This is expressed as [14]:

$$\sigma_r = \sigma_0 \int_0^\infty F(E) \psi(x, t) dE = \sigma_0 \psi_0(x_0, t_0) \quad (1)$$

where  $\sigma_0 = 2\pi\lambda^2 g\Gamma_0/\Gamma$  is the peak cross section of a nonbroadened nuclear level whose total natural width is  $\Gamma$  and ground state width  $\Gamma_0$ . The Gaussian function  $F(E)$  is given by:

$$F(E) = (1/\Delta_s \pi^{1/2}) \exp[-(E - E_r + \delta)^2 / \Delta_s^2] \quad (2)$$

where  $\Delta_s$  is the Doppler width of the incident line of the  $\gamma$ -source and is defined by:

$$\Delta_s = E_s (2kT_s / M_s c^2)^{1/2}. \quad (3)$$

$E_s = E_r - \delta$  is the peak energy of the  $\gamma$ -line emitted by the  $^{53}\text{Cr}(n, \gamma)$  reaction; it is separated by an energy  $\delta$  from the resonance energy  $E_r$  of the nuclear level (after recoil correction).

In this resonance scattering process, free recoil of the emitting nucleus is assumed; the recoil energy is:  $E_R = E_r^2 / 2Mc^2 = 1.43$  keV and is far larger than the lattice energies of the sample.  $M_s$  is the mass of the

emitting isotope of the  $\gamma$ -source;  $T_s$  is the effective temperature of Cr defined by Lamb [15]. The function  $\psi(x, t)$  is a convolution between a Breit-Wigner resonance form and a Gaussian distribution of energies and is given by:

$$\psi(x, t) = \left( \frac{1}{2\sqrt{\pi t}} \right) \int_{-\infty}^{\infty} \frac{\exp[-(x-z)^2 / 4t]}{1+z^2} dz \quad (4)$$

$$\text{with } x = \frac{2|E - E_r|}{\Gamma}, \quad t = (\Delta_r / \Gamma)^2, \quad \Delta_r = E_r (2kT_r / M_r c^2)^{1/2} \quad (5)$$

where,  $E_r$ ,  $M_r$  and  $\Delta_r$  are related to the scatterer and are defined in a similar manner to that of the  $\gamma$ -source. In Eq. (1), the overlap integral was expressed as another  $\psi$  function where [14]:

$$x_0 = 2|E_r - E_s| / \Gamma = 2\delta / \Gamma \quad \text{and} \quad t_0 = (\Delta_s^2 + \Delta_r^2) / \Gamma. \quad (6)$$

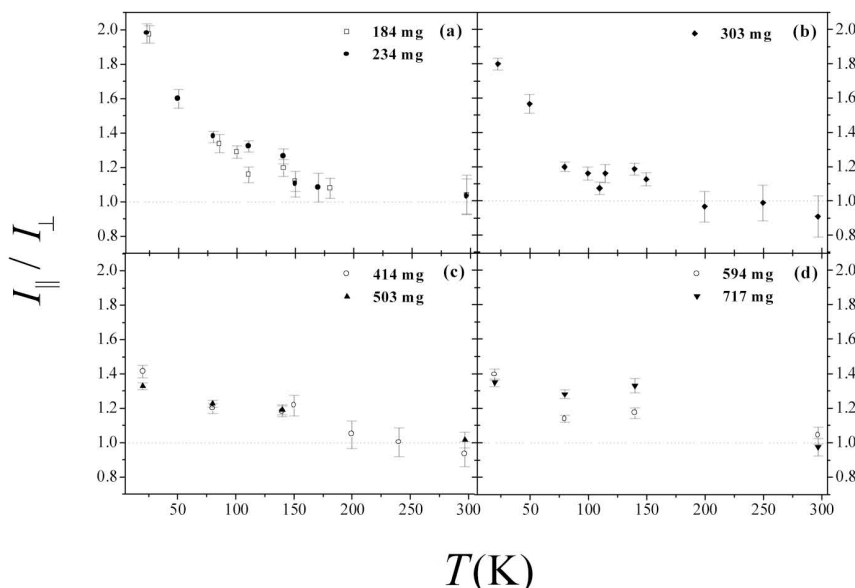
Thus the scattering cross section depends strongly on the effective temperatures  $T_s$  and  $T_r$  through the corresponding Doppler widths. The nuclear parameters for the calculations were taken from Table I of Ref. [16]. The Doppler width of the incident 6324 keV line was taken to be 8.3 eV, corresponding to the actual temperature,  $T \approx 460$  K, of the  $\gamma$ -source during reactor operation.

## 4. Results and Discussion

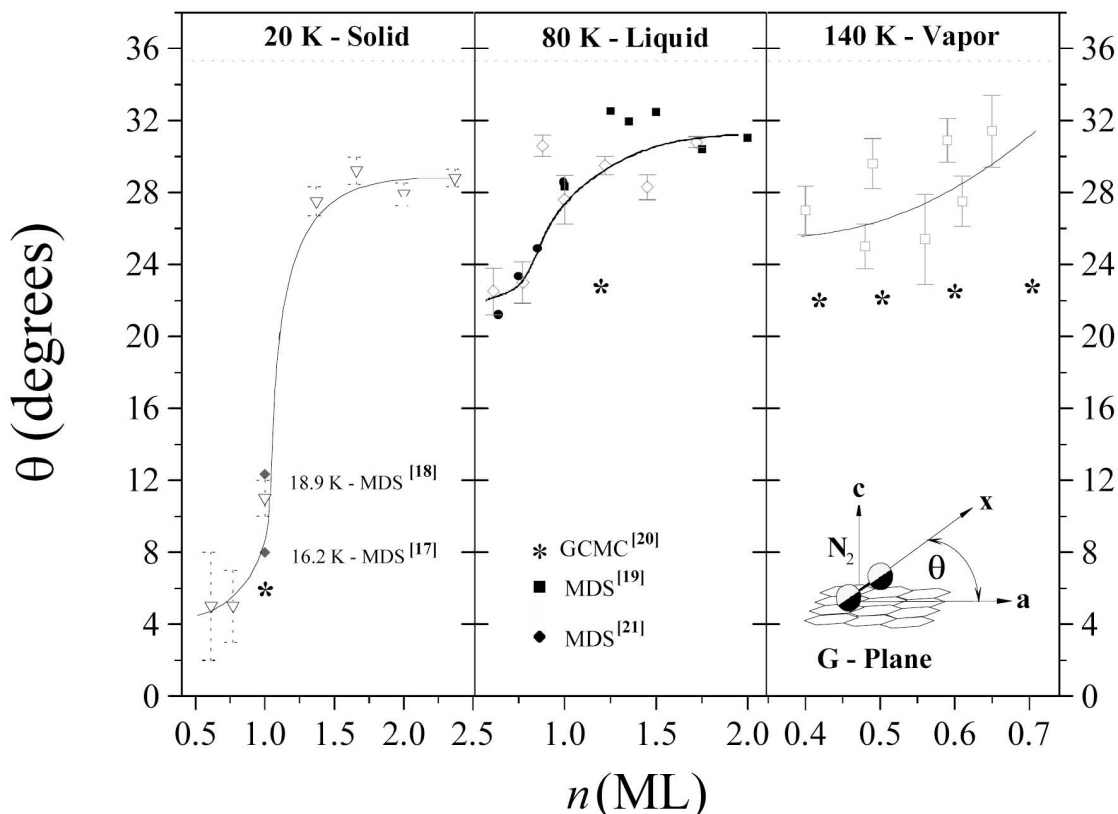
### 4.1 The N<sub>2</sub>+Grafoil Sample

The spectra of the resonantly scattered intensities from the 6324 keV level of the <sup>15</sup>N-containing samples have the same features but differ in intensity and in the signal/noise ratio. In Fig. 3 we show typical scattering spectra after background subtraction from the N<sub>2</sub>+Grafoil sample, at 20 K, using a 150 cm<sup>3</sup> HPGe detector, for the two perpendicular geometries of the cell. The scattering intensities reveal a high anisotropy,  $R = 1.97$ , which means that the adsorbed N<sub>2</sub> molecules lay nearly flat on the graphite surface. Figure 4 summarizes the measured values of  $R$  vs  $T$  for the different initial gas amounts in the cell. A value  $R = 1.0$  means that the N<sub>2</sub> molecules are randomly oriented relative to the planes of the graphite foils. Figure 4 shows that  $R$  decreases significantly with increasing  $T$  and also with the amount of gas for coverages above 1 ML. Thus  $R$  decreases to  $R \approx 1.30$  at 80 K and  $\approx 1.20$  at 140 K. This trend continues to  $R = 1.0$  at  $T \geq 180$  K, where the N<sub>2</sub> librational amplitude becomes very large. In the vapor phase, the N<sub>2</sub> occurring in the Grafoil region consists of an adsorbed part and a free nonadsorbed part. Above 80 K, the adsorbed part was determined by measuring the scattered intensities from the Grafoil compartment as a function of  $T$ . The data were then corrected to account for the fact that the scattered intensity from a constant amount of N<sub>2</sub> decreases with  $T$  [1,2]. We thus found that at 140 K the adsorbed gas fraction within the

irradiated compartment is between 70 % and 85 %, depending on the initial gas amount; the remaining amount occurs as a free nonoriented gas. Accounting for these fractions, the out-of-plane tilt angle was deduced from the measured  $R$  vs  $T$  and molecular coverage using the procedure of Ref. [2]. The results are depicted in Fig. 5, which shows the out-of-plane tilt angle versus molecular coverage for the solid (20 K), liquid (80 K) and vapor (140 K) phases. An outstanding result which emerges from Fig. 5 is the pronounced forward tilt of the N<sub>2</sub> molecule on the graphite surface at 140 K, where the gas is in the *vapor* phase and the N<sub>2</sub> is believed to stick loosely to the graphite surface. In general, good agreement is obtained between the NRPS values at 20 K and those obtained by n-diffraction experiments at 10.5 K [7]. Furthermore, molecular dynamic simulations (MDS) [17–20] seem to reproduce our measured data nicely at 20 K and 80 K (Fig. 5). For coverages above  $n = 1$  ML, some of the MDS tilt angles at  $\approx 80$  K are slightly higher than our measurements. It should be noted that the MDS values [19] have an estimated uncertainty of  $\pm 1.5^\circ$  at around  $\theta \approx 30^\circ$ . As for the vapor phase, no experimental data exist and the only available calculations, at 140 K, are those using the GCMC simulations [21] which yield lower values than our measured data (Fig. 5). This deviation is probably due to the fact that the GCMC calculations assume a geometrically flat surface which neglects the surface corrugations of graphite. This latter factor is important and when included as was done in the MDS, increases the predicted



**Fig. 4.** Measured ratios,  $R = I_{\parallel}/I_{\perp}$ , of the scattered intensities from the N<sub>2</sub>+Grafoil sample vs  $T$ . The initial gas amounts are indicated in each case: an amount of 303 mg of N<sub>2</sub> corresponds to a complete commensurate monolayer (ML) on graphite. Other coverages correspond to submonolayer or to coverages higher than 1 ML. Dotted lines ( $R = 1$ ) represent randomly oriented N<sub>2</sub>.



**Fig. 5.** Deduced tilt angles,  $\theta$ , of the  $N_2$  molecular axis with respect to the graphite planes as a function of molecular coverage for 20 K, 80 K, and 140 K (corresponding to the solid, liquid and vapor phases). Solid lines were passed through our measured data points (shown as open symbols with error bars) to lead the eye. The n-diffraction results at 10.5 K are labeled by full triangles. All other solid symbols (diamonds, circles, squares and stars) refer to theoretical calculations, where references are indicated. The inset at the bottom right corner defines the out-of-plane tilt angle  $\theta$  of  $N_2$  relative to the graphite planes.

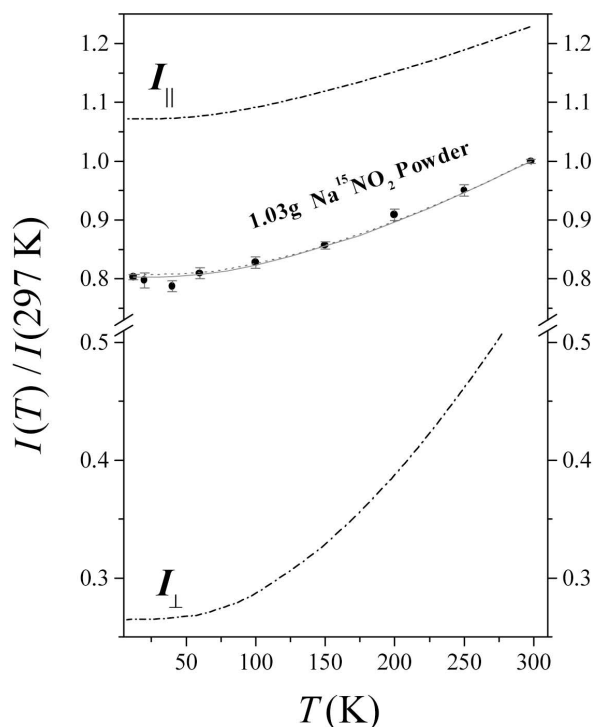
tilt angle, bringing it in much closer agreement with the measured values. Furthermore, the MDS results at lower temperatures, 20 K and 80 K (Fig. 5) which agree nicely with the present data also yield larger tilt angles than those of the GCMC. It would be interesting to extend the MDS calculations to 140 K to find out whether the present NRPS tilt angles can also be reproduced.

## 4.2 The $NaNO_2$ Samples

### 4.2.1 Temperature Variation of the Scattered Intensities in $NaNO_2$

The measured  $T$  dependence (relative to 297 K) of the scattered intensity  $I(T)$  from  $^{15}N$  in the isotopic powdered  $Na^{15}NO_2$  sample is shown in Fig. 6; it drops monotonically with  $T$ , reaching a plateau below 50 K. This reveals a quantum effect caused by the zero-point motion of the N-atom in the crystal where the Doppler width of the 6324 keV level in the  $^{15}N$  scatterer reaches near its minimum value. The solid curve is calculated

by assuming a Debye type behavior [22] for the external vibrational modes where a best fit to the data was obtained using a Debye temperature of  $\Theta_0 = 320$  K. In another calculation (dotted curve) the external modes were taken from Ref. [12]. Both calculations reveal a good agreement with the data points. The other two lines of Fig. 6 (labeled  $I_{\parallel}$  and  $I_{\perp}$  show the calculated relative intensities with the photon beam set parallel and perpendicular to the nitrite plane of an assumed single crystal. The scattering intensities are defined as  $I_{\parallel} = (I_b + I_c)/2$  and  $I_{\perp} = I_a$ , where  $I_a$ ,  $I_b$ ,  $I_c$  are the scattering intensities along the  $a$ ,  $b$ , and  $c$ -axes of the single crystal (where  $b$  and  $c$  are defined in Fig. 1 and  $a$  is along the normal to the  $(b, c)$  plane [12]). All curves in Fig. 6 are normalized to the scattered intensity from the powdered sample at 297 K denoted  $I(297\text{ K})$ , where  $I = (I_a + I_b + I_c)/3$ . Note the huge decrease of  $I_{\perp}$  with  $T$  as compared with the relatively small drop of  $I_{\parallel}$ . This again illustrates the effect of the zero-point motion which for the case of  $I_{\parallel}$  (representing the scattered intensity from the planar modes) is much larger than that of  $I_{\perp}$ .



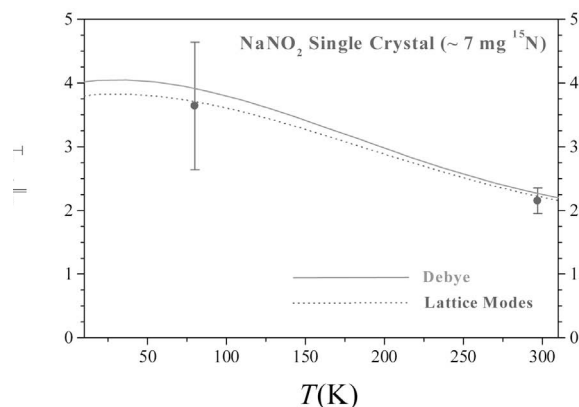
**Fig. 6.** Temperature variation of the scattered intensities relative to 297 K from the 1.03 g powdered  $\text{Na}^{15}\text{NO}_2$  sample. The solid line is a best fit calculated with a Debye temperature  $\theta_0 = 320$  K, while the dotted curve was calculated using the lattice frequencies [12]. The upper and lower curves are the calculated intensities  $I_{\parallel}$  and  $I_{\perp}$  relative to  $I(297\text{ K})$  of the powdered sample.

#### 4.2.2 Anisotropy Ratios in $\text{NaNO}_2$ Single Crystal

The measured scattered intensity ratios,  $R = I_{\parallel}/I_{\perp}$ , are given in Fig. 7 for 80 K and 297 K together with those calculated using a Debye temperature,  $\theta_0 = 320$  K (solid line). The dotted curve was calculated using the experimental lattice frequencies [12]. It may be seen that the above two calculations nicely reproduce the measured data points. Since we did not attempt to align the single crystal along either the  $b$  or  $c$  axis, we took the value of  $I_{\parallel}$  as  $I_{\parallel} = (I_b + I_c)/2$ . This procedure introduced an uncertainty of around 10 % in the calculated value which is far lower than the experimental error at 80 K. The relatively small error bar at 297 K is caused not only by the higher counting rate at 297 K but also because at 80 K, two cryostat radiation shields were used which increased the background at the detector.

#### 4.2.3 Comparison With Other Systems

It is interesting to compare the present results with other anisotropic systems such as  $\text{C}_{24}\text{Rb} + ^{15}\text{N}_2$ , in which the  $\text{N}_2$  molecules are adsorbed within the Rb planes of the graphite intercalation compound  $\text{C}_{24}\text{Rb}$ . In this case,



**Fig. 7.** Measured scattered intensity ratios,  $R = I_{\parallel}/I_{\perp}$  at 80 K and 297 K with the photon beam parallel and perpendicular to the *nitrite* planes of the single crystal. The solid and dotted curves correspond to calculations using the Debye and lattice mode models discussed in the text.

a high anisotropy ratio  $R \approx 2.8$  was measured [4] at 140 K; it is caused by the fact that the  $\text{N}_2$  molecules are adsorbed with their molecular axes nearly parallel to the graphite planes and because the  $\text{C}_{24}\text{Rb}$  sample was prepared using highly oriented pyrolytic graphite (HOPG). In another example [3],  $^{15}\text{NO}_2$  gas was adsorbed on Grafoil where a large anisotropy was expected. However, only a small ratio  $R \approx 0.97$  was measured between 297 K to 12 K. The reason could be traced down to the formation of dimers,  $\text{N}_2\text{O}_4$ , that are adsorbed with their  $\text{N}=\text{N}$  molecular axis perpendicular to the graphite planes which drastically reduced the anisotropy [3]. In yet another system, a *nitrate*  $\text{Na}^{15}\text{NO}_3$  single crystal was used [23] and the measured ratio was  $\approx 1.43$  at 295 K, to be compared with  $R = 2.15$  measured here for  $\text{NaNO}_2$ . The reduced anisotropy is caused by the fact that one of the six internal modes of the planar  $\text{NO}_3^-$  ion is vibrating along the normal to the nitrate plane which increased the scattered intensity  $I_{\perp}$ . This is in contrast to the *nitrite* case where all the *internal* modes are planar, with no component along the perpendicular direction.

## 5. Conclusions

We used the NRPS technique to study the molecular orientations in the  $\text{N}_2$ +Grafoil system and in a single crystal of sodium nitrite. This was done by monitoring the zero-point motion of the N-atom, occurring in these two molecular forms. We have shown that the NRPS method is a powerful tool for measuring the properties of adsorbed molecules on graphite and for testing MDS and MC calculations of adsorbed gases. It may also be used for checking the phonon spectra in solids and the lattice modes in molecular crystals measured by infrared and Raman methods.

## Acknowledgments

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